

For the problems below, **approximate the acceleration of gravity as -10 m/s^2** . (We're on Earth.) The point of this practice is not highly precise answers but rather building up your intuition and mental-math abilities. (And let's not bother putting a directional \mathbf{j} aside each vector quantity.)

1. A ball was thrown upward at 40 m/s . (This is almost 90 mph , which is ridiculous. Some baseball players can throw a ball this fast, although not upward.) The data table below shows the velocity at one-second intervals.

time (s)	velocity (m/s)
0.0	40.00
1.0	30.00
2.0	20.00
3.0	10.00
4.0	0.00
5.0	-10.00
6.0	-20.00
7.0	-30.00
8.0	-40.00

- a. At what time has the ball reached its peak?
 $t = 4 \text{ s}$ ($v_f = at + v_i : 0 = -10t + 40$)
- b. At its peak, what is the ball's *acceleration*?
 $a = -10 \text{ m/s/s}$
- c. What is the ball's displacement in that first second?
 $\Delta x = v_{\text{avg}}t = \frac{1}{2}(40+30)1 = 35 \text{ m}$
- d. What is the ball's total displacement, over the 8.0 seconds?
 $\Delta x = v_{\text{avg}}t = \frac{1}{2}(40+-40)8 = 0 \text{ m}$
- e. What total distance (not displacement) does the ball travel, over the 8.0 seconds?
distance up = $|\frac{1}{2}(40+0)4| = |80 \text{ m}| = 80 \text{ m}$
distance down = $|\frac{1}{2}(0+-40)4| = |-80 \text{ m}| = 80 \text{ m}$
total distance = $2(80 \text{ m}) = 160 \text{ m}$

2. A ball was thrown upward at 60 m/s .

- a. How many seconds does it take to reach its peak?
 $t = 6 \text{ s}$
- b. How many seconds does it take to return to its starting height?
 $t = 12 \text{ s}$
- c. What is the acceleration of the ball at 4.0 seconds?
 $a = -10 \text{ m/s/s}$
- d. What is the velocity of the ball at 8.0 seconds?
 $v = -20 \text{ m/s}$ ($v_f = at + v_i : v_f = -10(8) + 60$)
- e. How high does the ball travel? (This is another way of asking for its displacement, when it's at its peak.)
 $\Delta x = v_{\text{avg}}t = \frac{1}{2}(60+0)6 = 180 \text{ m}$
- f. What is the displacement of the ball between $t = 1.0$ and $t = 3.0$ seconds?
 $\Delta x = v_{\text{avg}}t = \frac{1}{2}(50+30)2 = 80 \text{ m}$ (the " t " in the model represents a time interval, not a particular time; if the initial time is $t = 0$, then there is no meaningful difference between the two concepts; in this problem, there is a meaningful difference)

3. A ball was thrown downward at 20 m/s, over a deep hole.
- What is the velocity of the ball at 3.0 seconds?
 $v = -50 \text{ m/s}$
 - What is the acceleration of the ball at 3.0 seconds?
 $a = -10 \text{ m/s/s}$
 - What is the displacement of the ball at 3.0 seconds?
 $\Delta x = v_{\text{avg}}t = \frac{1}{2}(-20 + -50)3 = -105 \text{ m}$
4. A ball was thrown upward at 25 m/s.
- How many seconds does it take to reach its peak?
 $t = 2.5 \text{ s}$ ($v_f = at + v_i : 0 = -10t + 25$)
 - At its peak, what is the ball's acceleration?
 $a = -10 \text{ m/s/s}$
 - At its peak, what is the ball's velocity?
 $v = 0 \text{ m/s}$
 - What is its velocity upon returning to its original height?
 $v = -25 \text{ m/s}$ (due to symmetry, but also $v_f = -10(5) + 25$)
 - How high does the ball travel?
 $\Delta x = v_{\text{avg}}t = \frac{1}{2}(25 + 0)2.5 = 31.25 \text{ m}$
 - What is the ball's displacement at 4.0 seconds?
 $\Delta x = v_{\text{avg}}t = \frac{1}{2}(25 + -15)4 = 20 \text{ m}$